Design of HPCF with nearly zero flattened Chromatic Dispersion

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Abstract—Here we have consider an air-silica honeycomb lattice and demonstrate a new approach to the formation of a core defect. The honeycomb lattice has recently been suggested for the formation of a photonic band-gap guiding silica-core. Here we discuss how a core defect can be formed by manipulating the cladding region rather than the core region itself. There are so many difficulties occur during the design process. Because when parameters are being changed the designing varies accordingly. For this purpose we have use HPCF in scalar effective index method (SEIM) and consider chromatic dispersion of HPCF for having air hole diameter 1.0 µm, and pitch 2.0 µm. The maximum pitch can be consider as 5.0 µm and air hole diameter is 9.0 µm. Transparent boundary condition (TBC) is proposed here for the calculation of Refractive index of HPCF.

Index Terms—Honeycomb PCF, Ultra flattened Dispersion, TBC, SEIM. Refractive index.

I. INTRODUCTION

In the recent scenario the photonic crystal fiber have attracted much attention because it exhibits many unique optical properties, such as single-mode operation over a wide wavelength range, large waveguide chromatic dispersion, or a high degree of freedom in design. Now a days, research is carried on photonic crystal fibers (PCFs) which are also called holey fibers [1,2]. The PCFs have a central region called core surrounded by periodic air holes which work as a cladding. The PCF technology is used to create a fiber with high nonlinear coefficient and zero chromatic dispersion.

Most photonic crystal fibers (PCFs) have been fabricated in silica glass. The value of refractive index of silica glass can be calculated by sellemier formula.

\[
\eta^2 - 1 = \sum \left( \frac{A\lambda^2}{\lambda^2 - \lambda_i^2} \right) \tag{1}
\]

And the total dispersion, \(D = D_M + D_W\), and the waveguide dispersion is defined as

\[
D_W = -\left(\frac{\lambda}{c}\right)\frac{d^2}{d\lambda^2} n_{eff} \tag{2}
\]

Where \(\lambda\) is the operating wavelength and \(c\) is the velocity of light.

In this paper, the optical properties of solid core HPCF with different up/down doping levels are considered. The doping level of the core adds new freedom of solid core HPCF design,[3-5]. In optical communication, dispersion plays an important role as it determines the information carrying capacity of the fiber. Therefore it becomes important to study the dispersion properties of PCF.[6] To improve the accuracy different values for the effective core radius are used. The results show that the solid core HPCF has great potentials and dispersion compensation for air hole diameter \(d=1.0\mu m\), Pitch = 2.0 µm and layer = 7.

The optical properties of PCF have been used like Effective Index method (EIM), Scalar effective index method (SEIM).[3] The SEIM method is used for weak guiding approximation and accurate approximations. In the SEIM method the value selection for effective core radius of the PCF is important for the accuracy.[6,7] We calculate the effective refractive index of the fundamental mode \(n_{eff}\) of the PCF in the commonly used SEIM model the relative hole diameter \(d/A\) varying from 0.2 to 0.8.
The accuracy of this method is worth investigating as the weakly guiding approximation in the SEIM model is made invalid by the large index contrast between silica and air. The definition of the radius of the unit cell in calculating the effective cladding index and the fiber core of the corresponding approximate step-index fiber remain ambiguous and different values are used. [8-11] The novel fiber has a central low-index core region and a cladding consisting of a silica background material with air holes situated within a honeycomb lattice structure. The results for a honeycomb-based silica–air photonic crystal fiber are in very good agreement with the results from the other methods.[12]

II. SCALAR EFFECTIVE INDEX METHOD

In SEIM the effective cladding index of a hexagonal unit cell which consists a Fiber rod is calculated with respect to rod diameter and pitch (Λ), then the effective index of PCF is obtained by using the effective cladding index.[16]

One of the best suited analytical methods is scalar effective index method which is valid for the LP01 fiber mode based on weak-guidance approximation. Fundamental space-filling mode (FSM) of a PCF is considered to be the mode with the largest modal index of the infinite two-dimensional photonic crystal structure that surrounds the PCFs core. The core refractive index is supposed to be the same as the refractive index of core material which is given by the Sellmeier formula. But the refractive index of cladding material is obtained by using the effective cladding index and the fiber core of the approximate step-index fiber in terms of Seim Principle.

The Scalar wave equation is :

\[
[\Delta^2 + (k^2n^2 - \beta^2)] \Psi
\]

(3)

Used to obtain the effective cladding index. Here \( \Delta \) is the transverse laplacian operator in cylindrical coordinates, \( k=(\omega/c) \) is the wave number in Vacuum, \( n \) is the material index, and \( \beta \) is the propagation constant and \( \psi \) can be either the electric or magnetic field.

We can get the following equation in the inner and outer areas of the air hole under the assumption of weak guidance.

\[
K(\phi) \frac{\mathbf{J}_0[T(\phi)a]}{J_0(\phi_0a)} - \mathbf{J}_1[T(\phi)a] - Y_1[T(\phi)a]\frac{(\mathbf{J}_1[T(\phi)R]}{Y_1[\phi_0(R)\phi_0]} = 0
\]

(4)

Equal to

\[-T(\phi)\{J_1[T(\phi)a] - Y_1[T(\phi)a]\}\frac{(\mathbf{J}_1[T(\phi)R]}{Y_1[\phi_0(R)\phi_0]} = 0
\]

Where \( I, J, \) and \( Y \) are Bessel functions. The optimum radius for SEIM is \( R=\Lambda/2 \).[16]

In terms of \( \beta(\phi) \) we can find out the effective refractive index for Space filling mode. The hexagonal unit cell is approximated by a circular one of radius \( R \).

III. DESIGN PRINCIPLE

In this method consider that refractive index of silica is \( n_{core} \) is 1.45 and the effective core radius is \( a_{eff} = \Lambda/3 \) \( ^{0.5} \).

It is consider that the triangular PCFs can be well parameterized in terms of the \( V \) parameter and from \( V \) parameter we have

\[
V = \frac{2\pi}{\Lambda} a_{eff} (n_{core}^2 - n_{air}^2) \]

Where \( U = \frac{2\pi}{\Lambda} a_{eff} (n_{core}^2 - n_{air}^2) \) and 

\[
W = \frac{2\pi}{\Lambda} a_{eff} (n_{core}^2 - n_{air}^2) \]

The values of

\[
k^2(\phi) = \beta^2(\phi) - n_{air}^2 \phi^2/c^2
\]

(6)

\[
\gamma^2(\phi) = n_{silica}^2 \phi^2/c^2 - \beta^2(\phi).
\]

(7)

With \( c \) having the velocity of light in vacuum.

When we have solve the fundamental equation of SEIM for the propagation constant \( \beta(\phi) \) of the LP01 mode of approximate step index fiber

\[
\mathbf{u}(\phi) \frac{(\mathbf{J}_1[\phi]r_{core})}{\mathbf{J}_0[\phi]r_{core}} = \mathbf{w}(\phi) \frac{(\mathbf{K}_1[\phi]r_{core})}{\mathbf{K}_0[\phi]r_{core}}
\]

(8)

Where \( n_{core}(\phi) \) is the refractive index of the core and \( r_{c} \) is the core radius.

We have calculated fundamental space filling mode and the index guiding mode for different air hole sizes. Calculations have been done by using PCF parameters, hole to hole distance \( \Lambda = 2.0 \mu m \), core radius \( r_{c} = 0.64L \), air hole diameter \( d = 1.0 \mu m \).

Figure: 2. circular unit cell of hexagonal [16]
It is clear from the figure that as the air filling fraction increases the credibility of the SEIM reduces as the difference between the refractive index of the silica and the refractive index of the fundamental space filling mode increases, which is the foremost requirement of the weakly guided approximation.

IV. DISPERSION

It is phenomena in which the phase velocity of a wave depends on its frequency. From the calculation of dispersion for various combinations we have found that the proposed Honeycomb PCF structure is designed as shown in figure 3. The dispersion coefficient $D(\Lambda)$, which includes both waveguide and material dispersion, is proportional to the second derivative of effective index of guided mode with respect to ‘$\Lambda$’.

The Effective refractive index for silica glass HPCF is calculated and presented here for constant Pitch but having varying air hole diameter.

After this calculation is carried out for constant air hole diameter but this time Pitch is varying.
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Figure: 7. Refractive index for constant air hole diameter having varying pitch.
Again the calculation is carried out for constant air hole diameter (d= 1.0 µm) and for constant Pitch (2.0 µm), but this time rings are varying.

Figure: 8. Refractive index for Constant air hole diameter and constant Pitch.
The calculation of dispersion for honeycomb PCF for various hole diameter and pitch size is calculated and the result is shown below.

Figure: 9. shows the comparison of chromatic dispersion of proposed Honeycomb PCF when pitch is 2.0 µm.

Figure: 10. Comparison of chromatic dispersion of proposed Honeycomb PCF when air hole diameter is 1.0µm.
The result, so obtained, gives that the dispersion calculated for Honeycomb photonic crystal fiber using the Scalar index method gives best result in comparison of other structures. Here we have calculated the dispersion for various data but it shows that when we consider air hole diameter 1.0 µm and Pitch 2.0 µm and select the 7 layers then it gives best result. The fiber parameters are optimized to yield best agreement with available data. The discrepancy observed at higher wavelength values is due to the fact that the refractive index of the silica and the effective cladding index are wavelength dependent.

V. CONCLUSION

VI. ABBREVIATIONS AND ACRONYMS

HPCF: Honeycomb Photonic Crystal Fiber
TBC: Transparent Boundary Condition.
SEIM: Scalar Effective index method.
UFD: Ultra Flattened Dispersion.
RI: Refractive Index.
EIM: Effective Index method.
FSM: Fundamental space-filling mode.

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